UNIT 9

Areas and Volumes

- Pythagoras Theorem
- Area
- Volume

After completion of this unit, the students will be able to:

- > state Pythagoras theorem.
- solve right angled triangle using Pythagoras theorem.
- ▶ find the area of
 - A triangle when three sides are given (apply Hero's formula),
 - A triangle whose base and altitude are given.
 - . An equilateral triangle when its side is given.
 - A rectangle when its two sides are given.
 - · A parallelogram when base and altitude are given.
 - · A square when its side is given.
 - . Four walls of a room when its length, width and height are given.
- find the cost of turfing a square/rectangular field.
- ▶ find the number of tiles, of given dimensions, required to pave the footpath of given width carried around the outside of a rectangular plot.
- ▶ find the area of circle and a semi circle when radius is given.
- ▶ find the area enclosed by two concentric circles whose radii are given.
- ▶ solve real life problems related with areas of triangle, rectangle, square, parallelogram and circle.
- find the volume of:
 - · A cube when its edge is given.
 - · A cuboid when its breadth and height are given.
 - A right circular cylinder whose base radius and height are given.
 - A right circular cone whose radius and height are known.
 - A sphere and a hemisphere when radius is given.
- ▶ solve real life problems related to volume of cube, cuboid, cylinder, cone and sphere.

SUMMARY

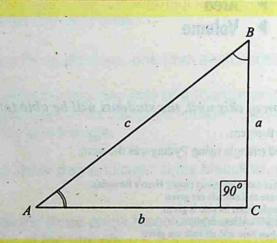
- 1- An angle bisector of a triangle is a line segment that bisects an angle of the triangle and has its other end on the side opposite to that angle.
- 2- Every triangle has three angle bisectors, one for each angle.
- 3- An altitude of a triangle is the line segment from one vertex, perpendicular to the opposite side.
- 4- Every triangle has three altitudes, one from each vertex.
- 5- A line-segment which bisects any side of a triangle and makes a right angle with the sides at its mid point is called the perpendicular bisector of the side of a triangle.
- 6- Every triangle has three perpendicular sides bisectors, one for each side.
- 7- The point at which the three angle bisectors of a triangle meet is called the incenter of the triangle.
- 8- The point at which the three altitudes of a triangle meet is called the orthocenter of the triangle.
- 9- The point of intersection of the three perpendicular bisectors of the sides of a triangle is called the circum-center of the triangle.
- 10- The point at which the three medians of a triangle meet is called the centroid of the triangle.
- 11- A line coplanar with a circle intersecting the circle at one point only is called the tangent line to the circle.

9.1 PYTHAGORAS THEOREM

Pythagoras Theorem:-

The square of the hypotenuse of a right triangle is equal to the sum of the squares of the two sides.

$$c^2 = a^2 + b^2$$



EXAMPLE-1

The sides of a right triangle are 5cm and 12cm. Find the hypotenuse.

SOLUTION: Given: a = 5cm, b = 12cm, Let the length of hypotenuse be c. Then by pythagoras theorem.

$$c^{2} = a^{2} + b^{2}$$

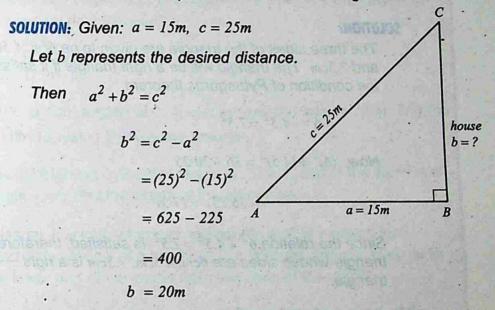
$$= (5)^{2} + (12)^{2}$$

$$= 25 + 144 = 169$$

$$c = 13cm$$

EXAMPLE-2

A 25m ladder leans against a house with its foot 15m from the house. How far is the top of the ladder from the ground?



EXAMPLE-3

If 30,72,78 represent the lengths of the sides of a triangle. Is triangle a right triangle?

SOLUTION: Given:
$$a = 30$$
, $b = 72$, $c = 78$

We have pythagoras theorem, it states: $c^2 = a^2 + b^2$

$$R.H.S = a^{2} + b^{2} = (30)^{2} + (72)^{2}$$

$$= 900 + 5184$$

$$= 6084$$

$$L.H.S = c^{2} = (78)^{2}$$

$$= 6084$$

$$R:H.S = L.H.S$$

Thus triangle is a right triangle.

EXAMPLE-4

The sides of a triangle are of lengths 6cm, 4.5cm and 7.5cm. Is this triangle a right triangle? If so, which side is the hypotenuse?

SOLUTION:

The three sides of the triangle are given to be 6cm, 4.5cm and 7.5cm. The triangle will be a right triangle if it satisfies the condition of Pythagoras theorem

$$6^2 + 4.5^2 = 7.5^2$$

Now
$$(6)^2 + (4.5)^2 = 36 + 20.25$$

$$=56.25 = (7.5)^2$$

Since the relation $6^2 + 4.5^2 = 7.5^2$ is satisfied, therefore, the triangle whose sides are 6cm, 4.5cm, 7.5cm is a right triangle.

Also
$$7.5^2 = 6^2 + 4.5^2$$

:. The side of length 7.5cm is the hypotenuse of the triangle.

FXERCISE - 9.1

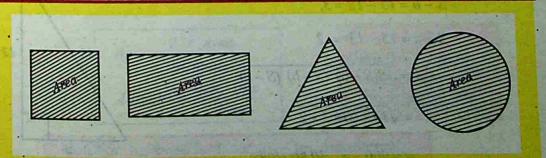
- 1- Find the third side of each right triangle with legs a and b and hypotenuse c.
 - (i) a=3, b=4, c=?
 - (ii) a = 5, c = 13, b = ?
 - (iii) b = 5, c = 61, a = ?
- 2- If the legs of a right triangle are 2ab and $a^2 b^2$, prove that the hypotenuse is $a^2 + b^2$.
- **3-** Find the hypotenuse of the right isosceles triangle each of whose legs is *l*.

ERRORE WITH B RE ADDRORS 2011

- 4- Find the hypotenuse of a right isosceles triangle whose legs are 8cm.
- 5- If the numbers represent the lengths of the sides of a triangle, which triangles are right triangles?
 - (i) 3, 4, 5
 - (ii) 9, 17, 25
 - (iii) 11, 61, 60
- 6- $\triangle ABC$ is right angled at C. If $m\overline{AC} = 9cm$ and $m\overline{BC} = 12cm$, find the length \overline{AB} , using Pythagoras theorem.
- 7- The hypotenuse of a right triangle is 25cm. If one of the sides is of length 24cm, find the length of the other side.
- 8- A ladder 17m long when set against the wall of a house just reaches a window at a height of 15m from the ground. How far is the lower end of the ladder from the base of the wall?
- **9-** The two legs of a right triangle are equal and the square of the hypotenuse is 50. Find the length of each leg.
- 10- The sides of a triangle are 15cm, 36cm and 39cm. Show that it is a right angled triangle.

9.2 AREAS

The surface inside the boundary of a shape is called area.



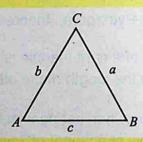
9.2.1 The Area of a Triangle

Area of a Triangle when all the three sides are given

A triangle ABC with sides a,b,c and

$$2S = a+b+c \implies S = \frac{a+b+c}{2},$$

where 'S' is half the perimeter of a triangle.



Then area of any triangle is $A = \sqrt{S(S-a) (S-b) (S-c)}$

This is called Hero's Formula for finding the area of a triangle.

EXAMPLE Find the area of a triangle whose sides are 5,12 and 13.

SOLUTION: Given:
$$a = 5, b = 12, c = 13$$
 then

$$2S = a + b + c$$

$$2S = 5 + 12 + 13 = 30$$
 \Rightarrow $S = 15$

$$S-a=15-5=10$$
.

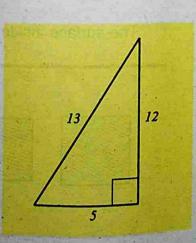
$$S-b=15-12=3$$

$$S-c=15-13=2$$

$$A = \sqrt{S(S-a) (S-b) (S-c)}$$

$$=\sqrt{15\times10\times3\times2}$$

$$=\sqrt{900} = 30 \text{ sq.units}$$



Note:- In this case, the triangle is a right triangle with base 5, altitude 12 and hypotenuse 13.

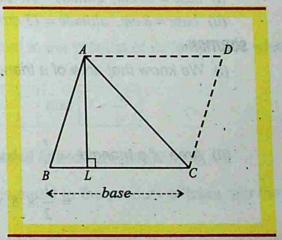
Hence area
$$(A) = \frac{1}{2} \times (base) \times (altitude)$$

= $\frac{1}{2}$ (5) (12) = $\frac{60}{2}$ $A = 30$ square unit.

Note: Area of a triangle is denoted by A.

Area of a Triangle when base and Altitude are given

Draw any triangle ABC as shown in the figure. Let \overline{BC} be its base and let $\overline{AL} \perp \overline{BC}$. Then \overline{AL} is the corresponding altitude. Through A and C draw line parallel to \overline{BC} and \overline{BA} respectively, intersecting each other at a point D. Then, clearly ABCD is a parallelogram with base \overline{BC} and corresponding altitude \overline{AL} .



Area of
$$\triangle ABC = \frac{1}{2}$$
 (Area of Parallelogram $ABCD$) $= \frac{1}{2} (\overline{BC} \times \overline{AL})$

$$= \frac{1}{2}(b \times h)$$
 (where b is the base and h is the altitude.)

Thus, we have Area of $\Delta = \frac{1}{2} \times Base \times Altitude$.

$$Base = \frac{2 \times Area}{Altitude}$$

$$Altitude = \frac{2 \times Area}{Base}$$

Altitude of a triangle is its height and denoted by 'h'.

Notation for base is 'b' and 'h' for the altitude.

EXAMPLE-1 Find the altitude of a triangle whose base is 16 cm and area is 34 cm²

SOLUTION: Altitude of the triangle =
$$\frac{2 \times Area}{base}$$

Here area =
$$34 \text{ cm}^2$$
 and base = 16 cm

Altitude =
$$\frac{2 \times Area}{Base} = \left(\frac{2 \times 34}{16}\right) = 4.25 \text{ cm}$$

IMPORTANT

The side opposite to a right angle in a right angled triangle is its hypotenuse.

EXAMPLE-2 Find the area of triangles whose

- (i) base = 18 cm, altitude = 3.5 cm
- (ii) base = 8 cm, altitude = 15 cm

SOLUTION:

- (i) We know that area of a triangle = $\frac{1}{2} \times base \times altitude$ = $\frac{1}{2} \times 18 \times 3.5 = 31.5 \text{ cm}^2$
- (ii) Area of a triangle = $\frac{1}{2} \times base \times altitude$ = $\frac{1}{2} \times 8 \times 15 = 60 \text{ cm}^2$

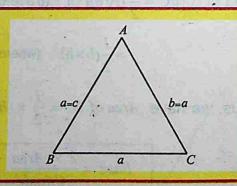
Area of an Equilateral Triangle when its side is given:-

In an equilateral $\triangle ABC$, a = b = c.

Therefore,
$$S = \frac{a+a+a}{2} = \frac{3a}{2}$$

$$S-a = \frac{a}{2} , S-b = \frac{a}{2} ,$$

$$S-c = \frac{a}{2}$$

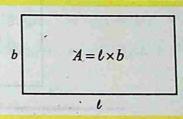


$$\Delta = \sqrt{S(S-a) (S-b) (S-c)} = \sqrt{\frac{3a}{2} \cdot \frac{a}{2} \cdot \frac{a}{2} \cdot \frac{a}{2}} = \frac{\sqrt{3} a^2}{4}$$

Thus area of an equilateral
$$\triangle ABC$$
 is $\frac{\sqrt{3} \ a^2}{4}$

Area of a Rectangle when its two sides are given

Consider a rectangle as shown in the figure.



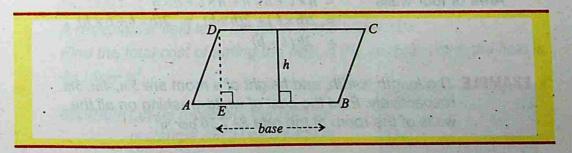
Length of the rectangle = lWidth of the rectangle = b.

The Area of a rectangle is equal to the product of its length and width. $A = \ell \times b$

Thus
$$b = \frac{A}{t}$$
 and $t = \frac{A}{b}$

Area of a Parallelogram when base and Altitude are given:-

The area of a parallelogram is equal to the product of base and the altitude drawn to the base.



Area of a parallelogram $ABCD = A = base \times altitude$

$$A = b \times h$$

Base =
$$b = \frac{A}{h}$$

Altitude =
$$h = \frac{A}{b}$$

IMPORTANT

Area of a triangle:

$$A = \frac{1}{2} \times base \times altitude$$

FARMA NO. 16

Area of a Square when its side is given:-

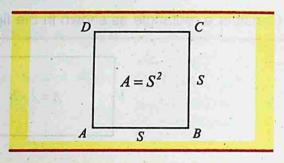
The area of a square *ABCD* is equal to the square of one of its sides.

$$A = Side \times Side$$

$$= S \times S = S^{2}$$

$$A = S^{2}$$

$$Side = S = \sqrt{A}$$

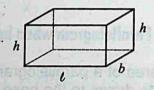


Unit of Area is square unit of length like: cm2, m2, km2.

Area of four Walls of a Room: A section will be a leading to the l

We can find the area of four walls of a room when its length, breadth and height are given.

Let length of the room = ℓ Width of the room = bHeight of the room = hArea of four walls = $h \times \ell + b \times h + h$



of four walls $= h \times l + b \times h + h \times l + b \times h$ $= 2(h \times l) + 2(b \times h) = 2(h \times l + b \times h)$ = 2h(l + b)

EXAMPLE The length, width, and height of a room are 5m, 4m, 3m respectively. Find the cost of white-washing on all the walls of the room at the rate Rs 7.50 per m².

SOLUTION: Given: $\ell = 5m$, b = 4m, h = 3m

Area of the four walls = $2(\ell + b) \times h = 2(5 + 4) \times 3$

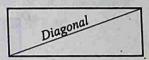
$$= 18 \times 3 = 54m^2$$

Therefore, cost of white-washing at the

rate of Rs $7.50/m^2 = 7.5 \times 54 = Rs 405$

Things to Remember:

- 1- Area of rectangle = (Length × Width)
- 2- Diagonal of a rectangle = $\sqrt{(Length)^2 + (Width)^2}$
- 3- Perimeter of a rectangle = 2(Length + Width)
- 4- Area of a square = a^2 where a = side of the square
- 5- Diagonal of a square = $\sqrt{2}a$
- 6- Area of a square = $\frac{1}{2}(Diagonal)^2$
- 7- Perimeter of a square = 4 × Side





25m

40m

9.2.2 Areas of Rectangular and Square Fields

Rectangular paths are generally around (outside or inside) a rectangular field or in the form of central paths. We shall explain the method to calculate their areas through some examples.

EXAMPLE-1

A rectangular field is of length 40m and width 25m.

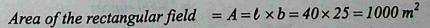
Find the total cost of turfing the field, if the cost of turfing the field is

Rs. 16per m2.

SOLUTION: Let us represent the field by rectangle ABCD as shown in the figure.

Length of the rectangular field = 40m

Width of the rectangular field = 25m



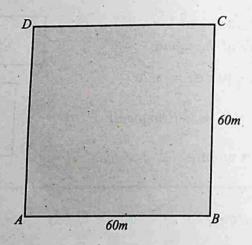
Rate of turfing = Rs. 16per m^2

 $Total\ cost = 16 \times 1000 = Rs.\ 16000$

EXAMPLE-2

The boundary of a square field with side of 60m. Find the area of the field.

Also find the cost of turfing the square field at the rate of Rs 5.00 per m^2



SOLUTION:

Let us represent the square field by ABCD as shown in figure.

Length of the side of the square field = 60m

Area of the square =
$$A = side \times side$$

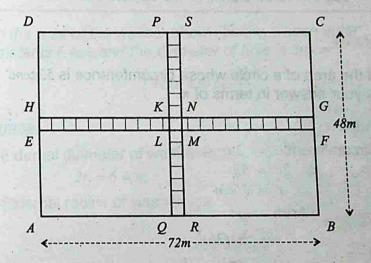
= 60×60
= $3600m^2$

Rate of turfing the square field = Rs. 5per m^2 $\therefore Cost of turfing the square field = 3600 \times 5$ = 18000 rupees

9.2.3

EXAMPLE-3

Two cross roads, each 2m wide, run at right angles through the center of a rectangular park of length 72m and width 48m such that each is parallel to one of the sides of the rectangular field. Find the area of the roads. Also find the number of tiles required to beautify this road where each tile having area of $4m^2$.



SOLUTION:

In figure, rectangular field ABCD represents the park and rectangle PQRS and EFGH represent the roads.

Area of the roads = Area of PQRS + Area EFGH - Area of KLMN

$$= [(48 \times 2) + (72 \times 2) - (2 \times 2)]m^{2}$$

$$= (96 + 144 - 4)m^{2}$$

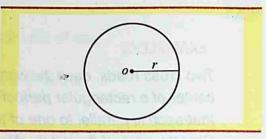
$$= 236 m^{2}$$

:. Number of tiles required =
$$\frac{236}{4}$$
 = 59 tiles

9.2.4 Area of a Circle

The circumference of circle = $2\pi r$ where the radius of the circle is r'.

Area of a circle = πr^2



Note: In examples and exercises, where π is not specified, use the value stored in the calculator.

EXAMPLE

Find the area of a circle whose circumference is $52\pi cm$. Give your answer in terms of π .

SOLUTION:

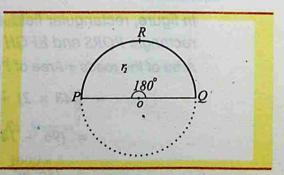
Circumference =
$$2\pi r = 52\pi$$

 $\Rightarrow 2r = 52$
 $\Rightarrow r = 26cm$
Area = πr^2
= $\pi (26)^2$
= $676\pi cm^2$

Area of a Semicircle:-

A semicircle is half of a circle, bounded by a diameter and half of the circumference.

Also a sector with an angle of 180° at the center of the circle is a semicircle.



In the figure,

Length of arc $PQ = \frac{1}{2}$ of the circumference of the circle.

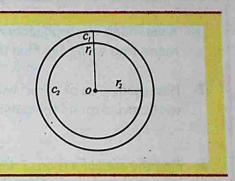
Area of sector $PRQ = \frac{1}{2}$ of the area of the circle.

Area of semicircle =
$$\frac{1}{2}(\pi r^2)$$
.

AREAS AND VOLUMES UNIT - 9

9.2.5 Area of Concentric Circles

Circles with same center but different radii are called concentric circles. In the figure, c_1 , c_2 are two concentric circles with same center 'O' but different radii r_1 and r_2 .



EXAMPLE

Find the area of the washer shown below, whose outer diameter is 6.4cm and the diameter of hole is 3.6cm.

$$\left(Take \pi to be \frac{22}{7}\right)$$

SOLUTION:

External diameter of washer is

$$2r_1 = 6.4cm$$

External radius of washer, $r_l = \frac{6.4}{2}$

$$r_1 = 3.2cm$$

Internal radius of washer =
$$r_2 = \frac{3.6}{2} = 1.8cm$$

∴ The area of the washer =
$$\pi r_1^2 - \pi r_2^2$$

= $\pi (3.2)^2 cm^2 - \pi (1.8)^2 cm^2$
= $\pi \Big[(3.2)^2 - (1.8)^2 \Big] cm^2$
= $\pi (10.24 - 3.24) cm^2$
= $(\pi \times 7) cm^2$

 $=\frac{22}{7}\times7=22cm^2$

FXERCISE - 9.2

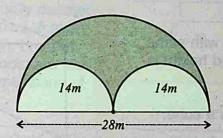
- 1- A verandah 40m long, 15m wide is to be paved with stones each measuring 6m by 5m. Find the number of stones.
- 2- How many tiles of $40cm^2$ will be required to pave the footpath 1m wide carried round the outside of a grassy plot 28m by 18m?
- 3- Find the area of a room 5.49m long and 3.87m wide. What is the cost of carpeting the room if the rate of carpet is Rs 10.50 per m^2 ?
- 4- The area of a rectangular rice field is 2.5 hectares and its sides are in the ratio 3:2. Find the perimeter of the field.
- 5- The area of a square playground is $4500 m^2$. How long will a man take to cross it diagonally at the speed of 3km per hour?
- 6- The diagonal of a square is 14cm. Find its area.
- 7- Find the area of a triangle whose sides are.
 - (i) 120cm, 150cm and 200cm
 - (ii) 50dm, 78dm and 112dm
- 8- The perimeter of a triangular field is 540m and its sides are in the ratio 25:17:12. Find the area of the triangle. Hint: Let the sides be 25x, 17x, 12x meters. Then $25x + 17x + 12x = 540 \Rightarrow 54x = 540 \Rightarrow x = 10$ The sides are 250m, 170m, 120m
- 9- Find the area of a parallelogram if its two adjacent sides are 12cm and 14cm and diagonal is 18cm.

Hints:

Let ABCDisa||^m in which $m\overline{AB} = 12$ cm, $m\overline{BC} = 14$ cm, $m\overline{AC} = 18$ cm Find area of \triangle ABC.

Area of ||" = 2(Area of \(\Delta \) ABC)

- 10- Find the area of the following washers whose external and Internal diameters are:
 - (i) 15cm and 13cm (ii) 1.2m and 0.9m
 - (iii) 40mm and 33mm.
- 11- Find the area of the shaded region.



- 12- Find the area of an equilateral triangle whose side is 8m.
- 13- The side of an equilateral triangle is 6cm. Find its area.
- 14- Find the area of the right triangle with legs 12cm and 35cm.
- 15- The base of a rectangle is three times its altitude. The area is $147cm^2$. Find the dimensions of the rectangle.
- **16-** Find the base of the parallelogram whose attitude is 18cm and whose area is $3m^2$.
- 17- The area of a parallelogram is $144cm^2$. Find the altitude if the base is $2m \log n$.
- 18- Find the area of the rectangle 2m long and 18cm wide.
- 19- The area of an equilateral triangle is $4\sqrt{3}$ cm². Find the length of a side.

9.3 VOLUMES

In this topic we study some figures which are not plane. The simplest of these figures are cubes and cuboids. These figures do not lie completely in a plane, such figures are called solids, (three dimensional figures).

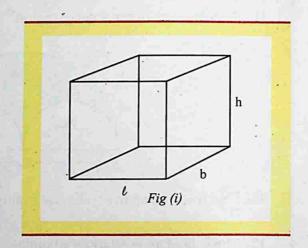
Cube and Cuboid

Cube :-

A six faces figure, with same length, breadth and height is called a cube.

The given figure is a cube,

Length of the cube = ℓ Breadth of the cube = bHeight of the cube = hwhere $\ell = b = h$, therefore.



Volume of a cube
$$=V = \ell \times \ell \times \ell$$

or $V = \ell^3$ cubic unit

EXAMPLE

Find the volume of the cube whose edge is 8m.

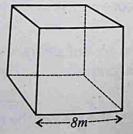
SOLUTION:

Given edge of the cube = 8m

$$Volume = \ell^3$$

$$V = 8 \times 8 \times 8 = 8^3$$

$$V = 512 \, m^3$$



Dimensions:

Length has <u>one dimension</u>. Area has <u>two dimensions</u>. Volume has <u>three dimensions</u>.

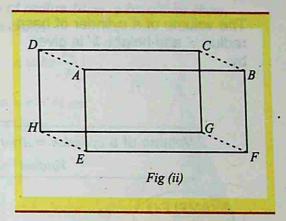
Cuboid :-

A six faces figure which has length, breadth and height is called cuboid,

(or rectangular parallelopiped).

Figure (ii) represents a cuboid.

The length, breadth and height of a cuboid are usually denoted by the letter symbols ℓ , b and h respectively. Length, breadth and height of a cuboid are also called the three dimensions of the cuboid.



Volume of a cuboid of length ℓ , breadth b and height h is $V = \ell \times b \times h$

EXAMPLE

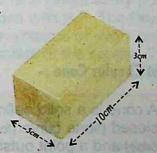
Find the volume of a block of wood whose length, breadth and height are respectively 10cm, 5cm and 3cm.

SOLUTION:

Given:

Length of the block of wood = 10cmBreadth of the block of wood = 5cmHeight of the block of wood = 3cm

$$V = \ell \times b \times h$$
$$= 10 \times 5 \times 3$$
$$= 150 \text{ cm}^3$$



Volume of a Cuboid and a Cube :-

- 1- Length, breadth and height must be expressed in the same units.
- 2- From above formula, we also observe that:

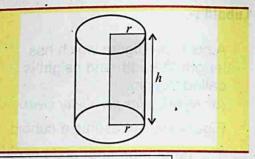
Length
$$\ell = \frac{v}{b \times h}$$

Breadth
$$b = \frac{v}{\ell \times h}$$

Height
$$h = \frac{v}{\ell \times b}$$

Volume of Right Circular Cylinder:

The volume of a cylinder of base radius r and height h is given by.



Volume of a cylinder = Area of base × height = $\pi r^2 \times h$ Volume = $\pi r^2 h$

EXAMPLE-1

Find the radius of the cylinder with volume 12320 cm³ and height 20 cm.

SOLUTION: Given
$$v = 12320 \text{ cm}^3$$
, $h = 20 \text{cm}$, $r = ?$

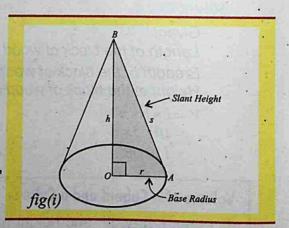
$$v = \pi \times r^2 \times h \implies r^2 = \frac{v}{\pi h}$$

$$r^2 = \frac{12320}{\frac{22}{7} \times 20} = \frac{12320 \times 7}{22 \times 20} = \frac{616 \times 7}{22} = 196$$

$$r = 14 \text{ cm}$$

Right Circular Cone:-

A cone is a solid defined by a closed plane curve (forming the base) and a point outside the plane (the vertex). A right circular cone can be generated by rotating the right-angled triangle BOA as shown in fig(i) about \overline{OB} , which represents the height of the cone. The base of the cone is a circle with radius \overline{OA} .



B is the vertex of the cone and \overline{BA} is the slant height.

Volume of a $cone = \frac{1}{3} \times area of base \times height$

Volume of a cone =
$$v = \frac{1}{3}\pi \times r^2 \times h$$

EXAMPLE

A cone has a circular base of radius 14cm, a height of 48cm, calculate the volume of the cone.

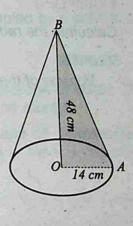
SOLUTION:

$$\left(Take \pi to be \frac{22}{7} \right)$$

Given radius of the base = r = 14 cm Height of the cone = h = 48cm

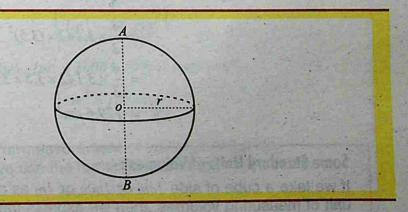
Volume of the cone =
$$\frac{1}{3}\pi r^2 h$$

= $\frac{1}{3} \times \frac{22}{7} \times (14)^2 \times 48$
= $\frac{1}{3} \times \frac{22}{7} \times 196 \times 48$
= $9856cm^3$



Sphere :-

A sphere is a body or space bounded by surface where every point on the surface is equidistant from a fixed point with in it. The fixed point is called the center of the sphere. The distance of every point on the surface to the fixed point is called the radius of the sphere. This radius is usually denoted by 'r'.



Volume of the sphere
$$=\frac{2}{3}\times 2\pi r^3$$

 $V=\frac{4}{3}\pi r^3$, where r is the radius of the sphere.

UNIT - 9 AREAS AND VOLUMES

Hemispheres :-

If a sphere is cut into half, the two portions are called hemispheres.

EXAMPLE-1

Calculate the radius of a sphere of volume 850 m^3 take π to be $\frac{22}{7}$

SOLUTION:

Volume of the a sphere =
$$850 \text{ m}^3$$

Radius =?
Now
$$V = \frac{4}{3}\pi r^3$$

$$r^3 = \frac{3V}{4\pi} \Rightarrow r^3 = \frac{3 \times 850 \times 7}{4 \times 22}$$

$$\Rightarrow r^3 = 202.8409$$

$$\Rightarrow r = (202.8409)^{\frac{1}{3}} = 5.88m$$

EXAMPLE-2

Find the volume of a sphere with radius 3.5cm.

SOLUTION:

Radius of a sphere
$$= r = 3.5cm$$

Volume of a sphere $= V = \frac{4}{3}\pi r^3$
 $= \frac{4}{3} \times 3.142 \times (3.5)^3$
 $= \frac{4}{3} \times 3.142 \times 3.5 \times 3.5 \times 3.5$
 $V = 179.6 cm^3$

Some Standard Units of Volumes:-

If we take a cube of side lcm or lm or lm as a standard unit of measuring volumes, then we express the volume as:

cubic centimeters: $(cm)^3$ cubic millimeters: $(mm)^3$ cubic meters: $(m)^3$

Real Life Problems Related to Volume

A solid region has a magnitude or size or measure. The measure or magnitude of a solid region is called its volume.

In other words, the measure of the space occupied by a solid is called its volume.

For example, consider the real life problems.

- A rectangular overhead tank is built for storage of water. The greater the volume the more water can be stored.
- A rectangular tin box is to be made to store oil. The greater the volume of the cuboidal region, the more is the quantity of oil it can store.

Remember that:

1- As
$$1cm = 10mm$$
,
Therefore, $1cm^3 = 10 \times 10 \times 10 \text{ m m}^3$
 $1cm^3 = 1000 \text{ m m}^3$

$$1m^{3} = 100 \times 100 \times 100 \text{ cm}^{3}$$
$$= 1000000 \text{ cm}^{3}$$
$$1m^{3} = 10^{6} \text{ cm}^{3}$$

Also
$$1m^3 = 1000 \times 1000 \times 1000 \text{ mm}^3$$

 $1m^3 = 10^9 \text{ mm}^3$

3- For measurement of volumes of liquids, we use the terms liters (t) and milliliters (ml).

$$1cm^{3} = 1m\ell$$
 $1000 cm^{3} = 1\ell$
and $1 m^{3} = 10000000 cm^{3} = 10000 \ell$
 $1 m^{3} = 1k\ell \ (1 \text{ kiloliter})$

EXAMPLE-1

Find in liters, the volume (capacity) of a storage tank whose length, breadth and depth are respectively 6.3m, 4.5m and 3.6m.

SOLUTION:

Length of the tank = 6.3 m

Breadth of the tank = 4.5 m

Height of the tank = 3.6 m

Volume of the tank = $\ell \times b \times h = 6.3 \times 4.5 \times 3.6m^3$

 $=102.06 \, m^3$

Volume of the tank $(m^3) = 102.06 \times 100 \times 100 \times 100$

 $=102060000 \, cm^3$

= $102060 \, litres \quad (:.1000 \, cm^3 = 1 \, litre)$

EXAMPLE-2

Capacity of a tank is 60kl. If the length, breadth of the tank are respectively 5m, and 4m, find its depth.

SOLUTION:

Volume of the tank $= 60 k t = 60000 liter = 60m^3$

Length of the tank = 5 m

Breadth of the tank = 4 m

Let depth of the tank = d

Now, volume of the tank = $length \times breadth \times depth$

Therefore, depth of the tank = $\frac{volume}{length \times breadth}$

$$= \frac{60}{20} (:60000 lt = 60 m^3)$$

=3m

FXERCISE - 9.3

Find the Volume of the Solids

- 1- A cube of a side 4cm.
- 2- A cube whose total area is $96cm^2$.
- 3- A rectangular box with length 4m breadth 3m and height 2m.
- 4- Right cylinder, with radius of base 4cm, altitude 10cm, use $\pi = \frac{22}{7}$
- 5- Circular cone, with radius of base 3cm, altitude 10cm.
- 6- Sphere, with radius 3cm.
- 7- Right circular cylinder, with circumferences of base 4cm, altitude 1m.
- 8- Cone with altitude 9cm, radius of base 6cm.

Review Exercise-9

I- Encircle the Correct Answer.

- 1. If the square of the hypotenuse of a right triangle is equal to the sum of the squares of the other sides, it is called:
 - (a) Pythagoras theorem
- (b) Scalene triangle
- (c) Equilateral triangle
- (d) Isosceles triangle
- 2. Area of a triangle when all the three sides are given is:
 - (a) $\frac{1}{2}bh$

- (b) bh
- (c) $\sqrt{s(s-a)(s-b)(s-c)}$
- (d) $\frac{a+b+c}{2}$
- 3. Area of an equilateral triangle with side 'a' is:
 - (a) $\frac{1}{2}bh$
- (b) bh
- $(c) \quad \frac{\sqrt{3}a^2}{4}$
- (d) $\frac{\sqrt{3}a^2}{2}$

Review Exercise-9									
4. Area of a rectangle is:									
	(a)	l×b			(b)	$\frac{1}{2} \times l$	+ <i>b</i>		
	(c)	$\frac{1}{3} \times l + b$			(d)	<i>l</i> ²			
5. Area of a square with side 'S' is:									Source John
	(a)	S	(b)	4S		(c)	2S	(d)	S^2
6. Area of a circle with radius 'r' is:									
	(a)	r^2	(b)	2πr		(c)	πr^2	(d)	$\pi^2 r$
7.	Are	a of a semi-	circl	e is:					
	(a)	$\frac{\pi r^2}{2}$	(b)	πr^2		(c)	$\pi^2 r$	(d)	2πr
8. Volume of a cube with edge 'l' is:									
	(a)	12	(b)	31		(c)	<i>l</i> ³ :	(d)	<i>1</i> ⁴
9. Volume of a right circular cylinder is:									
	(a)	$\frac{\pi r^2 h}{3}$			(b)	$\frac{\pi r^2 h}{2}$			
	(c)	$\pi r^2 h$			(d)	$\frac{4}{3}\pi r^2$			
7 -	Fill i	n the blanks.					Corred Resect	nii a	logica - t
If the square of the hypotenuse of a right triangle is equal to sum of the squares of the sides, then it is called theorem									
The surface inside the boundary of a shape is called									
Area of a triangle =									
Hero's formula for a triangle is $A = \underline{\hspace{1cm}}$.									

272

5. An equilateral triangle with side 'a' has area = \bot

6. Area of a rectangle = _

- 7. Area of a circle = _______
- 8. Volume of a cube with edge 'l' is _____.
- 9. Volume of a cuboid = ______.

SUMMARY Species to smule!

and the standard busban out an

scarta languageme early site yeabound out shisp soaps on a supply

TOTAL NAMED IS A COLOR OF THE PARTY.

Pythagoras Theorem: The square of the hypotenuse of a right triangle is equal to the sum of the squares of the legs.

Area: The space inside the boundary of a shape.

Area of a Triangle: $A = \frac{1}{2} \times base \times altitude$

Area of a Triangle: $A = \sqrt{s(s-a)(s-b)(s-c)}$

 $s = \frac{a+b+c}{2}$, a, b, c are the sides of a triangle.

Area of an equilateral triangle: $A = \frac{\sqrt{3}a^2}{4}$, where 'a' is the side of the triangle.

Area of a rectangle: $A = length \times breadth$.

Area of a square: $A = side \times side$.

Area of a parallelogram: $A = base \times altitude$.

Area of a circle: $A = \pi r^2$

Circumference of a circle: $C = 2 \pi r$

Area of a semi-circle: $A = \frac{1}{2}(\pi r^2)$

Area of a washer: $A = \pi \left[r_1^2 - r_2^2 \right]$ and a simple high a to employ 41

 r_i is the radius of outer circle.

r; is the radius of inner circle.

Volume: The space inside the boundary of a three dimensional shape.

Volume of a cube: $V = l^3, l$ is the length of edge.

is equest to the sum of the squares of the leas

Volume of a cuboid: $V = l \times b \times h$

l = length, b = breadth, h = height

Volume of a right circular cylinder: $V = \pi r^2 h$

h = height of the cylinder

A. Strengman luminships me to both

Time & selected to such

r = radius of the base

Volume of a right circular cone: $V = \frac{1}{3}\pi r^2 h$

h = height of the cone

r = radius of the base

Volume of sphere: $V = \frac{4}{3}\pi r^3$

Volume of a hemi-sphere: $V = \frac{2}{3}\pi r^3$

Are a particular and the second of the secon